

LESSON
5-5

Practice C
Complex Numbers and Roots

Solve each equation.

1. $\frac{1}{2}x^2 = -28$

2. $3x^2 + 14 = -19$

Find the zeros of each function.

3. $f(x) = x^2 - 6x + 20$

4. $g(x) = -2x^2 + 8x - 16$

5. $h(x) = x^2 - 2x + 3$

Find the values of x and y that make each equation true.

6. $6x - 2i = (-2y)i + 10$

7. $-40i + 2x = (5y)i - 12$

8. $-8y + 14i = (7x)i - 2$

Find each complex conjugate.

9. $\sqrt{3}i - 25$

10. $-5i + \frac{12}{5}$

11. $-2 - 1.5i$

Solve.

12. Does the function $f(x) = (x - 1)^2 + 5$ have real or imaginary zeros? How can you determine that without any calculations or graphing?

13. Joel wrote the function $s(t) = t^2 + 6t + 34$ to approximate the speed of a model rocket that he built. The function models the speed of the rocket, s , at a given time, t .

a. What does $s(t) = 0$ represent?

b. Solve the equation to find the zeros of the function.

c. Is Joel's function correct? Explain.

LESSON 5-5

Practice A

- $3i; 7i - 1; -2i$
- i
- -1
- a
- bi
- $2i$
- $9i$
- $-9i$
- $8i$
- $5i$
- $21i$
- $1 - 2i$
- $-5i$
- $2 + 3i$
- a. $x = \sqrt{-25}$, so $x = 5i$ and $-5i$.
b. Possible answer: You could multiply $(x + 5i)(x - 5i)$ to get the original expression.
- a. $x = \sqrt{-16}$, so $x = 4i$ and $-4i$.
b. Possible answer: You could multiply $(x + 4i)(x - 4i)$ to get the original expression.

Practice B

- $4i\sqrt{2}$
- $6i\sqrt{2}$
- $\frac{1}{3}i$
- $x = \pm 3i\sqrt{3}$
- $x = \pm i\sqrt{7}$
- $x = \pm 4i\sqrt{3}$
- $x = \pm i\sqrt{21}$
- $x = 4, y = 5$
- $x = -\frac{1}{3}, y = \frac{1}{2}$
- $x = 1 \pm i\sqrt{3}$
- $x = -3 \pm i\sqrt{5}$
- $-3 - i$
- $-4 - 3i$
- $-11i$
- $3 \pm i\sqrt{11}$

Practice C

- $x = \pm 2i\sqrt{14}$
- $x = \pm i\sqrt{11}$
- $x = 3 \pm i\sqrt{11}$
- $x = 2 \pm 2i$
- $x = 1 \pm i\sqrt{2}$
- $x = \frac{5}{3}, y = 1$
- $x = -6, y = -8$
- $x = 2, y = 0.25$
- $-25 - i\sqrt{3}$
- $\frac{12}{5} + 5i$
- $-2 + 1.5i$

- Imaginary; possible answer: since a is positive, the parabola opens upward and the vertex is at the minimum. Since the function is in vertex form, you can tell that the vertex is at $(1, 5)$. With a minimum at 5 , the function never crosses the x -axis, so the zeros have to be imaginary.
- a. The beginning and end of the flight when the speed of the rocket is 0
b. $t = -3 \pm 5i$
c. No; possible answer: the zeros are imaginary because the graph never crosses the x -axis so the function never equals 0 . The speed of the rocket must be 0 before takeoff and after landing.

Reteach

- $6i\sqrt{2}$
- $12i\sqrt{2}$
- $10i$
- $15i\sqrt{6}$
- $16i$
- $-7i\sqrt{2}$
- $9i$
- $1 - 4i$
- $12 + i$
- $x = \pm 3i\sqrt{2}$
- $x = \pm\sqrt{-4}$
 $x = \pm 2i$
- $x^2 = -49$
 $x = \pm\sqrt{-49}$
 $x = \pm 7i$
- $x^2 = -100$
 $x = \pm\sqrt{-100}$
 $x = \pm 10i$
- $x^2 = -36$
 $x = \pm\sqrt{-36}$
 $x = \pm 6i$
- $x^2 = -12$
 $x = \pm\sqrt{(4)(3)(-1)}$
 $x = \pm 2i\sqrt{3}$

Challenge

- $2i, -7i$
- $-6i, -8i$
- $9i, -12i$
- $5i, 49i$